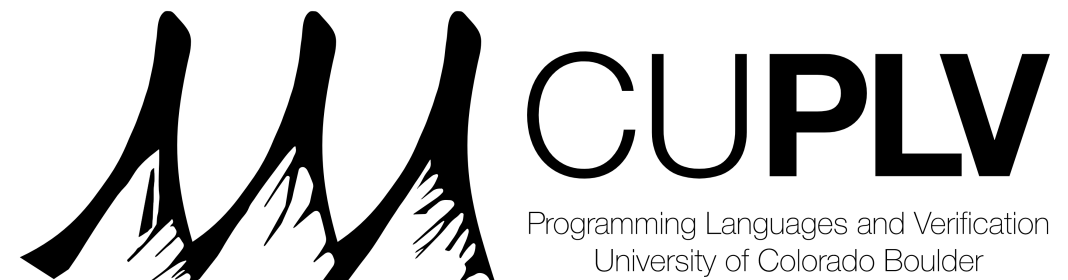


Static Analysis with Demand-Driven Value Refinement

Benno Stein, **Benjamin Barslev Nielsen**, Bor-Yuh Evan Chang & Anders Møller



Sound static analysis for JavaScript

- Static analysis for JavaScript is very challenging

o[m]()

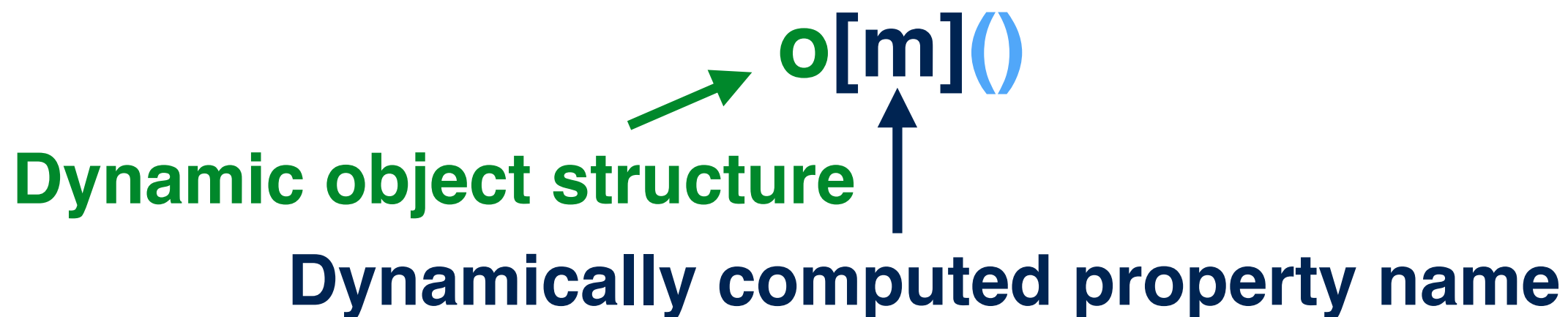
Sound static analysis for JavaScript

- Static analysis for JavaScript is very challenging

Dynamic object structure  **o[m]()**

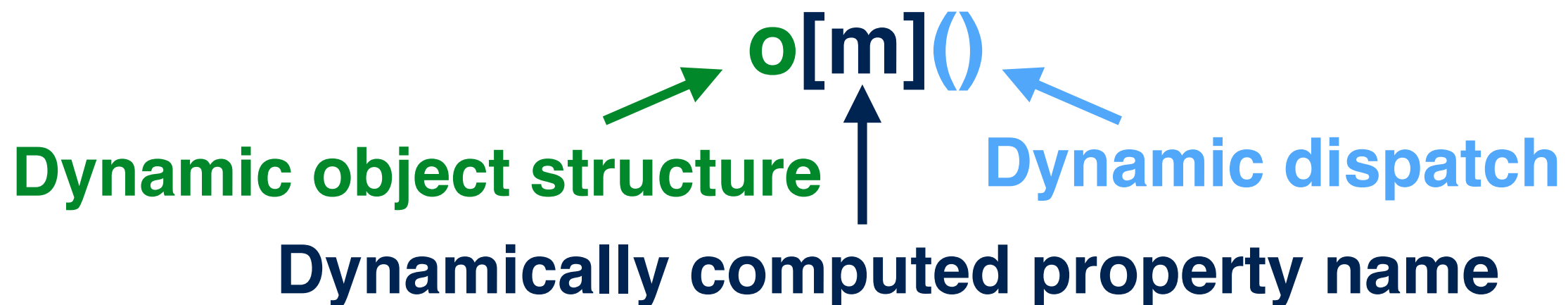
Sound static analysis for JavaScript

- Static analysis for JavaScript is very challenging



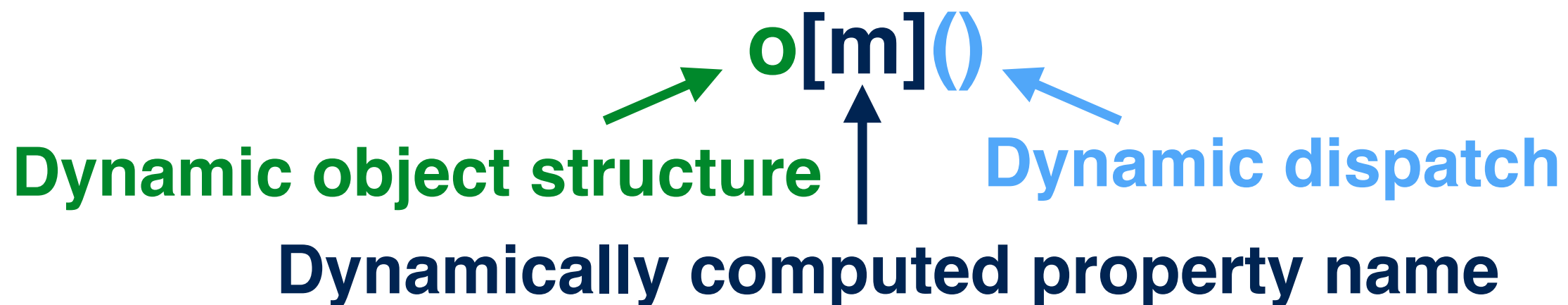
Sound static analysis for JavaScript

- Static analysis for JavaScript is very challenging



Sound static analysis for JavaScript

- Static analysis for JavaScript is very challenging



- Critical precision losses renders analysis useless
 - Too much spurious data-flow

State-of-the-art data-flow analyzers

- Fail to analyze load of some very popular libraries
 - Critical precision losses occur
- Common characteristics
 - Forwards whole program analysis
 - Tracks data-flow, e.g., strings, functions and other objects
 - Non-relational
 - Aims to mitigate critical precision losses by:
 - Context sensitivity
 - Syntactic patterns and special-case techniques

Critical code example

Example program

```
func = o1[name]
```

.

.

.

```
o2[name] = func
```

.

.

.

```
o2.foo(...)
```

Analysis state

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

Example program



$\text{func} = o1[\text{name}]$

.

.

.

$o2[\text{name}] = \text{func}$

.

.

.

$o2.\text{foo}(\dots)$

Critical code example

Analysis state

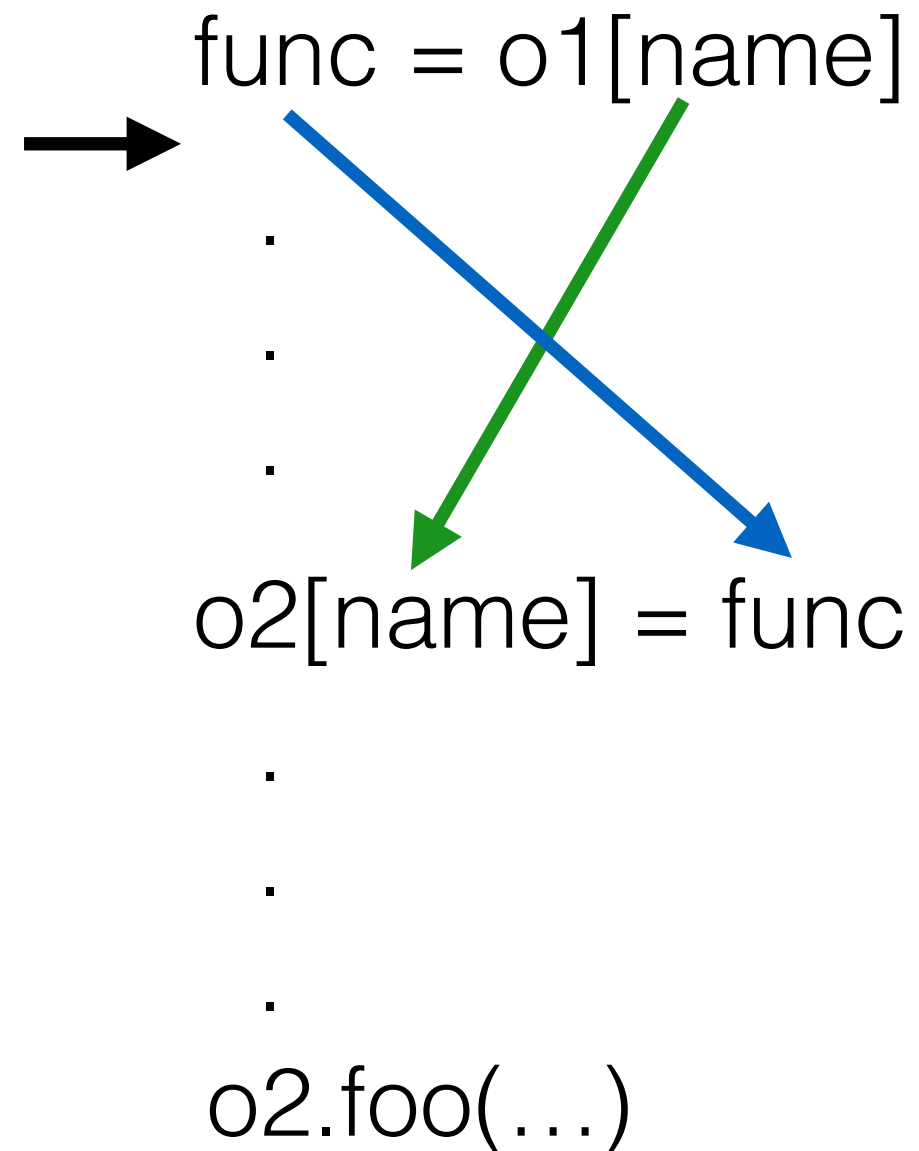
$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program



Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{ T_{\text{str}} : f1|f2 \}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.

$o2[\text{name}] = \text{func}$

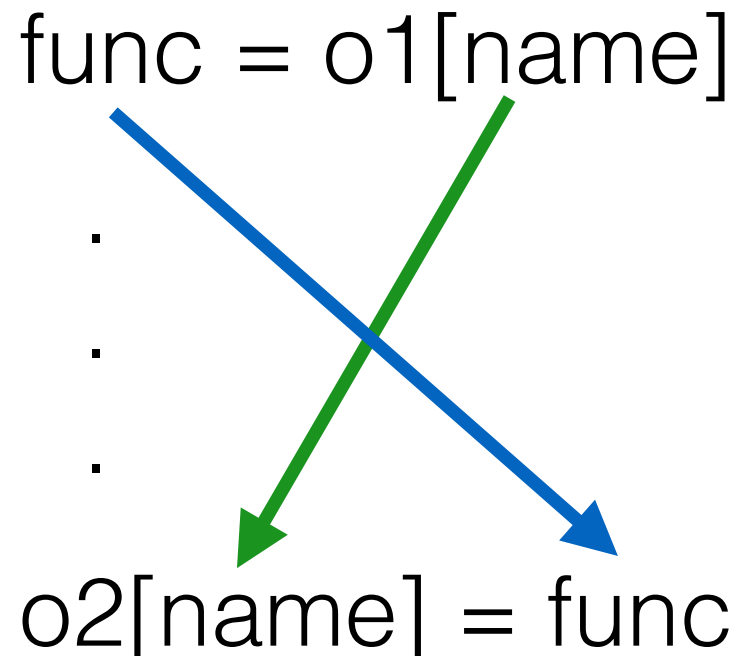
.

$o2.\text{foo}(\dots)$

Critical code example

Example program

```
func = o1[name]
.  
.  
.  
o2[name] = func
```



Analysis state

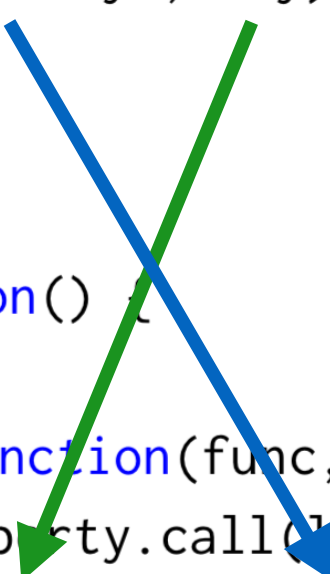
```
o1 = {foo: f1, bar: f2}
name = T_str
o2 = { T_str : f1|f2}
func = f1|f2
```

Resolves both f1 and f2

→ o2.foo(...)

The Lodash library

```
1 function baseFor(object, iteratee) {
2   ...
3   while (length--) {
4     var key = props[++index];
5     iteratee(object[key], key)
6   }
7 }
8
9 mixin(lodash, (function() {
10  var source = {};
11  baseFor(lodash, function(func, methodName) {
12    if (!hasOwnProperty.call(lodash.prototype, methodName)) {
13      source[methodName] = func;
14    }
15  });
16  return source;
17 }()));
```



Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

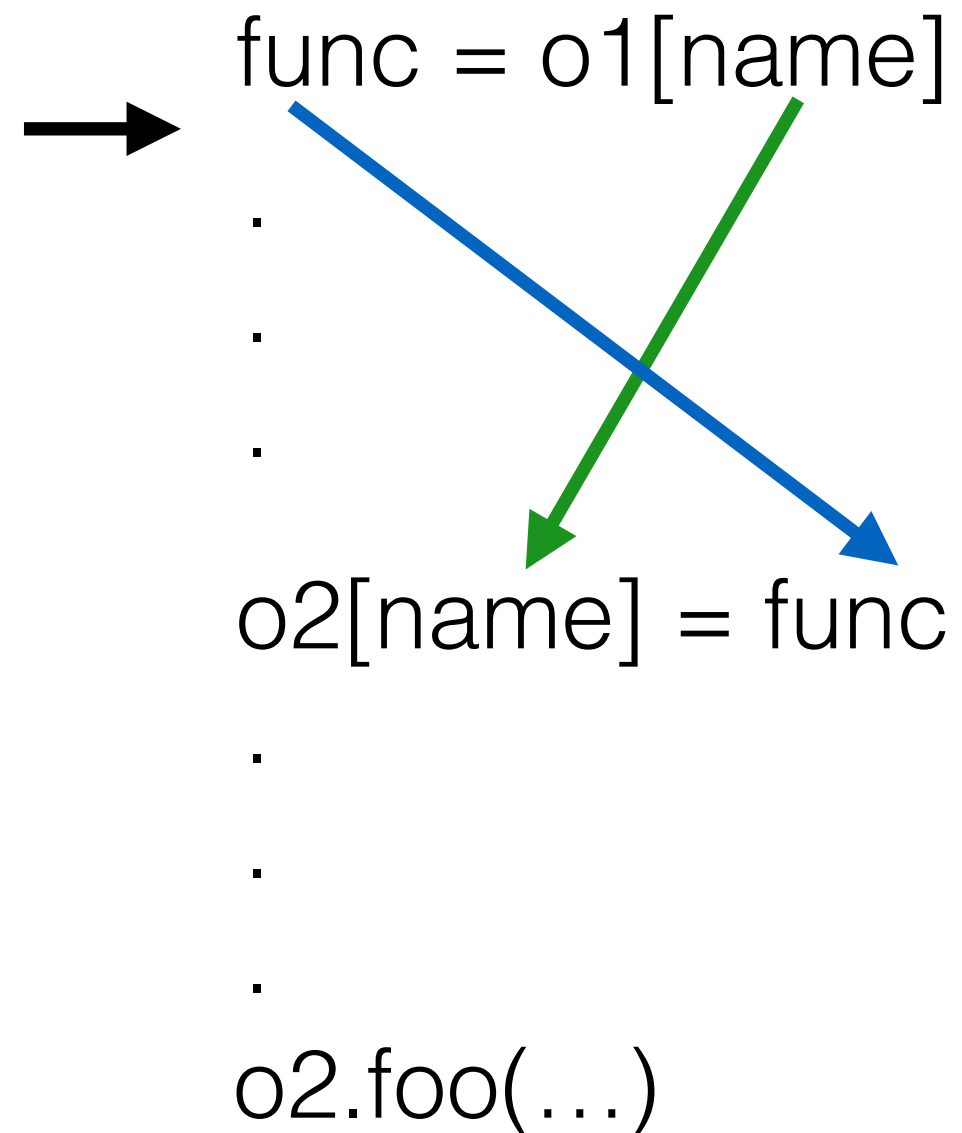
$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program

→ $\text{func} = o1[\text{name}]$
.
.
.
.
 $o2[\text{name}] = \text{func}$
.
.
.
 $o2.\text{foo}(\dots)$



Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.

.

.

→ $o2[\text{name}] = \text{func}$

.

.

.

$o2.\text{foo}(\dots)$

Demand-driven value refinement

Regain relational information through refinement queries

Without modifying base analysis domain

Refinement query: What is x , when $y \mapsto \hat{v}$?

What value can variable x have,
given that y has value \hat{v} ?

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.
. .
. . .



$o2[\text{name}] = \text{func}$

.
. .
. . .

$o2.\text{foo}(\dots)$

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.
. .
. . .

$o2[\text{name}] = \text{func}$

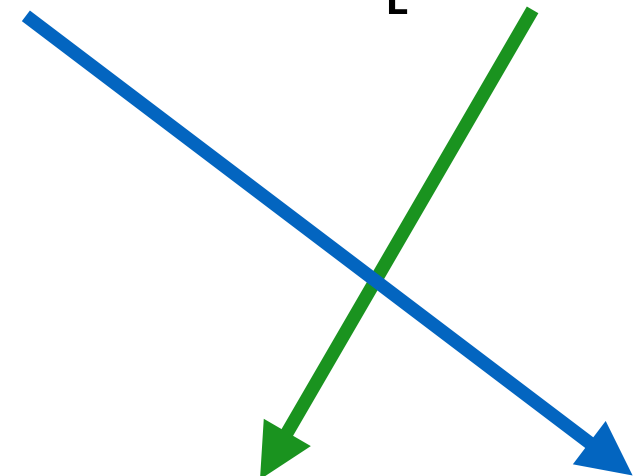
.
. .
. . .

$o2.\text{foo}(\dots)$

What is name, when $\text{func} \mapsto f1$?



What is name, when $\text{func} \mapsto f2$?



Backwards abstract interpreter for value refinement

- Backwards goal-directed from the query location
- Separation logic based abstract domain
 - Intuitionistic - constraints hold for all extensions
 - Special symbolic variable RES represents value being refined

symbolic variables	$\hat{x}, \hat{y}, \hat{z}, \text{RES}$	$\in \widehat{Var}$
symbolic stores	$\varphi \in \widehat{Store}$	$::= \hat{h} \wedge \pi \mid \varphi_1 \vee \varphi_2$
heap constraints	\hat{h}	$::= \text{true} \mid \text{unalloc}(\hat{x}) \mid x \mapsto \hat{x} \mid \hat{x}_1[\hat{x}_2] \mapsto \hat{x}_3 \mid \hat{h}_1 * \hat{h}_2$
pure constraints	π	$::= \text{true} \mid \hat{e} \mid \pi_1 \wedge \pi_2$
symbolic expressions	$\hat{e} \in \widehat{Expr}$	$::= \hat{x} \mid \hat{v} \mid \hat{e}_1 \oplus \hat{e}_2$

Backwards abstract interpreter for value refinement

- Based on refutation sound Hoare triples $\langle \varphi \rangle s \langle \varphi' \rangle$
- Refutation soundness:
For all concrete runs where φ' holds after s , the state before s must satisfy φ .
- Encoding refinement queries:

What is x , when $y \mapsto \hat{v}$? $\rightsquigarrow \langle x \mapsto \text{RES} * y \mapsto \hat{y} \wedge \hat{y} = \hat{v} \rangle$

Critical code example

func = o1[name]

→ o2[name] = func

Critical code example

Refinement query: What is name, when $\text{func} \mapsto f1$?

$\text{func} = o1[\text{name}]$

$\longrightarrow o2[\text{name}] = \text{func}$

Critical code example

Refinement query: What is name, when $\text{func} \mapsto f1$?

$$\text{func} = o1[\text{name}]$$
$$\langle \text{name} \mapsto \text{RES} * \text{func} \mapsto \widehat{\text{func}} \wedge \widehat{\text{func}} = f1 \rangle$$
$$\longrightarrow o2[\text{name}] = \text{func}$$

Critical code example

Refinement query: What is name, when $\text{func} \mapsto f1$?

$\langle \text{name} \mapsto \text{RES} * \text{o1} \mapsto \widehat{\text{o1}} * \widehat{\text{o1}} [\text{RES}] \mapsto \widehat{\text{func}} \wedge \widehat{\text{func}} = f1 \rangle$

$\text{func} = \text{o1}[\text{name}]$

$\langle \text{name} \mapsto \text{RES} * \text{func} \mapsto \widehat{\text{func}} \wedge \widehat{\text{func}} = f1 \rangle$

$\longrightarrow \text{o2}[\text{name}] = \text{func}$

Leveraging forwards analysis state

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\langle \text{name} \mapsto \text{RES} * o1 \mapsto \widehat{o1} * \widehat{o1}[\text{RES}] \mapsto \widehat{\text{func}} \wedge \widehat{\text{func}} = f1 \rangle$

Refinement result is the values of RES satisfying:

$$o1[\text{RES}] = f1$$

Refinement result: “foo”

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.
. .
. .

→ $o2[\text{name}] = \text{func}$

.
. .
. .

$o2.\text{foo}(\dots)$

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

What is name, when $\text{func} \mapsto f1$?

What is name, when $\text{func} \mapsto f2$?

Example program

$\text{func} = o1[\text{name}]$

.
. .
. .



$o2[\text{name}] = \text{func}$

.
. .
. .

$o2.\text{foo}(\dots)$

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = T_{\text{str}}$

$o2 = \{\}$

$\text{func} = f1|f2$

What is name, when $\text{func} \mapsto f1$?

“foo”

What is name, when $\text{func} \mapsto f2$?

“bar”

Example program

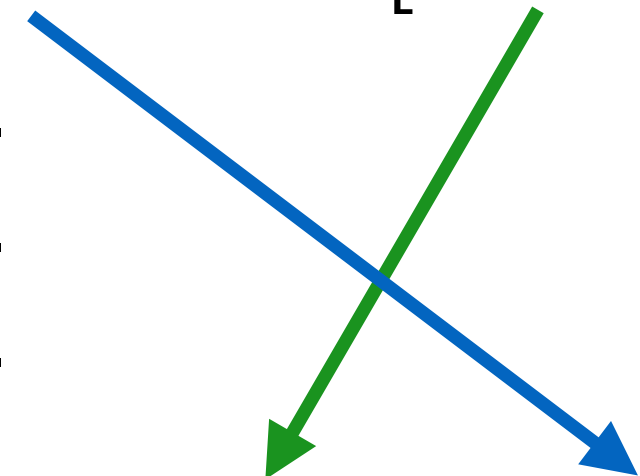
$\text{func} = o1[\text{name}]$

.
. .
. .

$o2[\text{name}] = \text{func}$

.
. .
. .

$o2.\text{foo}(\dots)$



Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = \top_{\text{str}}$

$o2 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{func} = f1|f2$

What is name, when $\text{func} \mapsto f1$?

“foo”

What is name, when $\text{func} \mapsto f2$?

“bar”

Example program

$\text{func} = o1[\text{name}]$

.
. .
. . .

$o2[\text{name}] = \text{func}$

.
. .
. . .

→ $o2.\text{foo}(\dots)$

Critical code example

Analysis state

$o1 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{name} = \top_{\text{str}}$

$o2 = \{\text{foo}: f1, \text{bar}: f2\}$

$\text{func} = f1|f2$

Example program

$\text{func} = o1[\text{name}]$

.
. .
. .

$o2[\text{name}] = \text{func}$

What is name, when $\text{func} \mapsto f1$?

“foo”

What is name

“bar”

Resolves only f1

→ $o2.\text{foo}(\dots)$

Implementation for JavaScript

- **TAJS_{VR}**: **TAJS** extended with demand-driven value refinement
- **TAJS** is a state-of-the-art analyzer for JavaScript
 - Implemented in Java
 - Active research since 2009
- **VR_{JS}**: Backwards abstract interpreter for JavaScript for answering refinement queries
 - Implemented in Scala from scratch



Compared to state-of-the-art

	#tests	TAJS	CompAbs	TAJS_{VR}
Underscore ¹	182	0 %	0 %	95% (2.9s)
Lodash3 ¹	176	0 %	0 %	98% (5.5s)
Lodash4 ¹	306	0 %	0 %	87% (24.7s)
Prototype ²	6	0 %	33% (23.1s)	83% (97.7s)
Scriptaculous ²	1	0 %	100% (62.0s)	100% (236.9s)
jQuery ³	71	7% (14.4s)	0 %	7% (17.2s)
JSAI tests ⁴	29	86% (12.3s)	34% (32.4s)	86% (14.3s)

“x% (y)” means succeeded x% of test cases with average time y

1: Most popular functional utility libraries

2: Wei et al. [2016]

3: Andreassen and Møller [2014]

4: Kashyap et al. [2014] & Dewey et al. [2015]

Compared to state-of-the-art

	#tests	TAJS	CompAbs	TAJS _{VR}
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Lodash4 ¹	306	0 %	0 %	87% (24.7s)
Prototype ²	6	0 %	33% (23.1s)	100% (17.2s)
Scriptaculous ²	1	0 % (12.0s)	34% (32.4s)	86% (14.3s)

TAJS_{VR} succeeds analyzing 92% of Underscore and Lodash tests, which all are unanalyzable by existing analyzers

“x% (y)” means succeeded x% of test cases with average time y

1: Most popular functional utility libraries

2: Wei et al. [2016]

3: Andreasen and Møller [2014]

4: Kashyap et al. [2014] & Dewey et al. [2015]

Value refinement insights

- Value refinement is triggered in few locations
 - In Lodash4, it is triggered in 7 locations in >17000 LoC
- Almost all queries are solved successfully (>99%)
- Queries are answered efficiently (Avg. ~10ms)
- Answering a query requires visiting few locations
 - Typically below 40
- Many queries requires interprocedural reasoning

Conclusion

- New technique: Demand-Driven Value Refinement
 - Relational reasoning on top of non-relational analysis
 - Eliminates critical precision loss on-the-fly
 - Uses backwards analysis for gaining relational precision
 - Exploiting forwards analysis state allows efficient refinements
- Experimental evaluation
 - First analysis capable of analyzing most popular JavaScript library
 - No significant overhead for incorporating backwards analyzer
 - Open-source: <https://www.brics.dk/TAJS/VR/>

Value refinement statistics

	Ref locs	Avg # queries	Succ (%)	Refiner time (%)	Avg query time (ms)	Avg. locs visited	Inter (%)
Underscore	5	268	99.98	22.4	2.43	5.05	0.10
Lodash3	12	475	99.99	47.2	5.46	10.47	40.22
Lodash4	7	1284	99.97	52.0	10.01	10.09	25.75
Prototype	4	188	100	2.5	13.08	39.98	48.10
Scriptaculous	2	601	100	3.4	13.21	36.91	42.26
JQuery	5	1	87.5	0.1	13.57	7.1	2.86
JSAI tests	0	-	-	-	-	-	-